FIITJEE

Diagnostic cum Scholarship Tests

SAMPLE PAPER
For Students of Class XII

Paper 4 Mathematical Olympiad, Physics & Astronomy Olympiad & Chemistry Olympiad

Duration : 120 minutes   **Paper Code: 1112-4**   *Maximum Marks : 168*

Please read the instructions and guidelines carefully :

Important Note : Please ensure to accurately input the details for the Question Paper Code as indicated at the top of this sheet (Side 2) into the corresponding columns / fields on the OMR sheet before proceeding with the paper. Incorrectly filled information regarding the class or paper may result in inaccurate outcomes or results.

> *"This paper has been scientifically designed to evaluate your potential – manifested and hidden for the target examinations mentioned in various sections of the paper. Thus, your adherence to the instructions is critical in the evaluation of the same"*

1. This Question paper consists of 3 sections.
2. Student should devote allotted time for each section. If a section is easy, then it is easy for everyone & was meant to be like that with a goal in mind. Do not switch over to another section if you find the section to be easy. If a section is tough, then it is tough for everyone. You are advised to spend 45 Minutes on Section-I, 45 Minutes on Section-II and 30 Minutes on Section-III. Opening the next section before completing the allotted time for the preceding section is not permitted. This adherence is crucial for assessing your true potential, as each section is meticulously crafted to evaluate your potential for the corresponding competitive examinations.
3. Candidate should open the seal of Section-II only after devoting 45 minutes on Section-I and Seal for Section-III is to be opened only after devoting 45 minutes on Section-II.
4. Sheets will be given to each candidate for rough work. Candidate must fill all details on the rough sheet and submit the same to invigilator along with OMR sheet. Candidate must mention the Question No. while doing the rough work in the sheet.
5. Please note candidates are not allowed to bring any prohibited items into the exam hall such as electronic devices, mobile phones, smart watch, earphones, calculators, books, notes, formula sheets, and bags.
6. Marking scheme is given in table below:

Section	Subject		Question no.	Marking Scheme for each question	
				Correct answer	**Wrong answer**
SECTION – I (Mathematical Olympiad) Time Allotted: 45 Minutess	MATHEMATICS	(PART-A)	1 to 10	**+3**	**–1**
	MATHEMATICS	(PART-B)	11 to 15	**+6 * Partial Marking**	**0**
SECTION – II (Physics & Astronomy Olympiad) Time Allotted: 45 Minutes	PHYSICS	(PART-A)	16 to 20	**+3**	**–1**
	MATHEMATICS	(PART-B)	21 to 25	**+3**	**–1**
	PHYSICS	(PART-C)	26 to 28	**+6 * Partial Marking**	**0**
	MATHEMATICS	(PART-D)	29 to 30	**+6 * Partial Marking**	**0**
SECTION – III (Chemistry Olympiad) Time Allotted: 30 Minutes	CHEMISTRY	(PART-A)	31 to 38	**+3**	**–1**
	CHEMISTRY	(PART-B)	39 to 42	**+6 * Partial Marking**	**0**

* Partial Marking: (Q. No. 11 to 15, Q. No. 26 to 30 & Q. No. 39 to 42):

Full Marks	**: +6**	If only (all) the correct option(s) is(are) chosen;
Partial Marks	**: +4.5**	If all the four options are correct but ONLY three options are chosen;
Partial Marks	**: +3**	If three or more options are correct but ONLY two options are chosen, both of which are correct;
Partial Marks	**: +1.5**	If two or more options are correct but ONLY one option is chosen and it is a correct option;
Zero Marks	**: 0**	If unanswered/incorrect option(s) chosen;

Section – I

Time: 45 Minutes

MATHEMATICS – (PART – A)

*This part contains **10 Multiple Choice Questions** number **1 to 10**. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.*

1. Which of the following is a null set?
    (A) $\{0\}$
    (B) $\{x: x > 0 \text{ or } x < 0\}$
    (C) $\{x : x^2 = 4 \text{ or } x = 3\}$
    (D) $\{x : x^2 + 1 = 0, x \in R\}$

2. The number of the real roots of the equation $|x+1|^2 + |x-5|^2 = \dfrac{27}{4}$ is

    (A) 2
    (B) 4
    (C) 6
    (D) 0

3. If $\log_4(x^2 + x) - \log_4(x+1) = 2,$ then the value of x is :

    (A) 1
    (B) 2
    (C) 4
    (D) 16

4. If $y = \log\left\{ \dfrac{x + \sqrt{(a^2 + x^2)}}{a} \right\}$, then the value of $\dfrac{dy}{dx}$ is

    (A) $\sqrt{a^2 - x^2}$
    (B) $a\sqrt{a^2 + x^2}$
    (C) $\dfrac{1}{\sqrt{a^2 + x^2}}$
    (D) $x\sqrt{a^2 + x^2}$

5. If $y = \ln(\sin\sqrt{x})$, then its first derivative is
    (A) $\dfrac{1}{2}\dfrac{\cot\sqrt{x}}{\sqrt{x}}$
    (B) $\dfrac{1}{2}\dfrac{\tan\sqrt{x}}{\sqrt{x}}$
    (C) $\dfrac{1}{2}\dfrac{\cos ec\sqrt{x}}{\sqrt{x}}$
    (D) $\dfrac{1}{2}\dfrac{\cos\sqrt{x}}{\sqrt{x}}$

6. If $a_i \in R$ and a_1, a_2, a_3 are in A.P., a_2, a_3, a_4 are in G.P. and a_3, a_4, a_5 are in H.P. then $\dfrac{a_1 - a_3}{a_3 - a_5}$ is equal to

    (A) $\dfrac{a_1}{a_3}$
    (B) $\dfrac{a_3}{a_1}$
    (C) $\dfrac{a_5}{a_1}$
    (D) 1

7. The absolute integral value of the solution of the equation $\sqrt{7^{2x^2-5x-6}} = \left(\sqrt{2}\right)^{3\log_2 49}$

   (A) 4   (B) 2
   (C) 6   (D) None of these

8. Number of integers satisfying $\left|x^2 - 3x + 2\right| = 3x - 2 - x^2$ is

   (A) 0   (B) 2
   (C) 6   (D) None of these

9. If points corresponding to the complex numbers z_1, z_2, z_3 and z_4 are the vertices of a rhombus, taken in order, then for a non-zero real number k
   (A) $z_1 - z_3 = i\, k(z_2 - z_4)$ (B) $z_1 - z_2 = i\, k(z_3 - z_4)$
   (C) $z_1 + z_3 = k(z_2 + z_4)$ (D) $z_1 + z_2 = k(z_3 + z_4)$

10. If z be any complex number such that $|3z - 2| + |3z + 2| = 4$, then locus of z is
    (A) an ellipse   (B) a circle
    (C) a line-segment   (D) None of these

MATHEMATICS – (PART – B)

*This part contains **5 Multiple Choice Multi Correct Type Questions** number **11 to 15**. Each question has 4 choices (A), (B), (C) and (D), out of which **MORE THAN ONE** are correct.*

11. $\triangle ABC$ is inscribed in $x^2 + y^2 = 16$ internal angular bisector of $\angle A$ intersects BC at D. If tangent drawn to circle at A intersects BC produced at P. If AB : AC = 3 : 2, then which of following is/are correct.

    (A) $\dfrac{PA}{PD} = 1$ (B) $\dfrac{PA}{PD} = \dfrac{3}{2}$

    (C) If $BC = \dfrac{5}{2}$, then PA = 3   (D) If $BC = \dfrac{5}{2}$, then PA = 4

12. If three positive unequal numbers a, b, c are in H. P., then
    (A) a + c > 2b   (B) $a^2 + c^2 > 2b^2$
    (C) $a^2 + c^2 > 2ac$ (D) None of these

13. If a, b and c are three terms of an A.P. such that $a \neq b$, then $\dfrac{b - c}{a - b}$ may be equal to

    (A) $\sqrt{2}$ (B) $\sqrt{3}$
    (C) 1   (D) 3

14. If one of the lines of $my^2 + \left(1 - m^2\right)xy - mx^2 = 0$ is a bisector of the angle between the lines $xy = 0$, then m is
    (A) 1   (B) 2
    (C) – 1/2   (D) – 1

15. If $\cos\beta$ is the geometric mean between $\sin\alpha$ and $\cos\alpha$, where $0 < \alpha, \beta < \pi/2$, then $\cos 2\beta$ is equal to

(A) $-2\sin^2\left(\dfrac{\pi}{4} - \alpha\right)$

(B) $-2\cos^2\left(\dfrac{\pi}{4} + \alpha\right)$

(C) $2\sin^2\left(\dfrac{\pi}{4} + \alpha\right)$

(D) $2\cos^2\left(\dfrac{\pi}{4} - \alpha\right)$

Section – II

Time: 45 Minutes

PHYSICS – (PART – A)

*This part contains **5 Multiple Choice Questions** number **16 to 20**. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.*

16. A particle is moving in a circle of radius $\dfrac{2}{3}$ m and mass of the particle is 2 kg. The kinetic energy of the particle depends on distance 'S' travelled by the particle as K.E. = $4S^4$. The angle made by net acceleration with the radial acceleration when the particle rotate by 60°, is

(A) $\tan^{-1}\left(\dfrac{3}{\pi}\right)$

(B) $\tan^{-1}\left(\dfrac{6}{\pi}\right)$

(C) $\tan^{-1}\left(\dfrac{1}{\pi}\right)$

(D) $\tan^{-1}\left(\dfrac{4}{\pi}\right)$

17. A person wants to drive on the vertical surface of a large cylindrical wooden 'well' commonly known as 'deathwell' in a circus. The radius of the 'well' is 2 meter, and the coefficient of friction between the tyres of the motorcycle and the wall of the well is 0.2 The minimum speed the motorcyclist must have in order to prevent slipping should be (take g = 10 m/s²)

(A) 10 m/s
(B) 15 m/s
(C) 20 m/s
(D) 25 m/s

18. A structure in the shape of letter *H* is formed with the help of three identical rods each of length *l*. The system can rotate along axis *l*. The angular speed of the system when plane of *H* becomes vertical from its original position of rest along the horizontal.

(A) $\dfrac{3}{2}\sqrt{\dfrac{g}{l}}$

(B) $\dfrac{2}{3}\sqrt{\dfrac{g}{l}}$

(C) $\dfrac{1}{3}\sqrt{\dfrac{g}{l}}$

(D) $\dfrac{3}{4}\sqrt{\dfrac{g}{l}}$

19. A body of mass m and radius r is released from rest along a smooth inclined plane of angle of inclination θ. The angular momentum of the body about the instantaneous point of contact on the incline from the instant of release is equal to

(A) mgrt cos θ
(B) mgrt sin θ
(C) (3/2) mgrt sin θ
(D) None of these
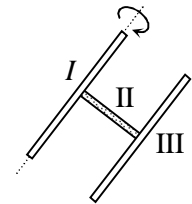
20. A bus can be stopped by applying a retarding force F when it is moving with speed $'v'$ on a level. road. The distance covered by it before coming to rest is $'s'$. If the load of the bus increases by 50% because of passengers, for the same speed and same retarding force, the distance covered by the bus to come to rest shall be

(A) 1.5 s   (B) 2 s

(C) 1 s   (D) 2.5 s

MATHEMATICS – (PART – B)

*This part contains **5 Multiple Choice Questions** number **21 to 25**. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.*

21. If $x^{18} = y^{21} = z^{28}$ where x, y, z are positive real numbers not equal to 1, then 3, $3\log_y x, 3\log_z y$ and $7\log_x z$ form an

(A) A.P   (B) G.P

(C) H.P   (D) None of these

22. If the point $P(2,-2)$ is the one end of the focal chord PQ of the parabola $y^2 = 2x$, then the slope of the tangent at Q is

(A) $\dfrac{-1}{2}$ (B) $\dfrac{1}{2}$

(C) -2 (D) 2

23. If a line passing through point $A(3,4)$ and having slope $\dfrac{2}{3}$ intersect circle $x^2 + y^2 = 9$ at points P and Q. Then AP.AQ is equal to

(A) 4   (B) 6

(C) 8   (D) 16

24. If $\displaystyle \lim_{x \to a} \tan\left(\dfrac{\pi x}{2a}\right) \cdot \sin\left(\dfrac{x-a}{2}\right) = \dfrac{2}{\pi}$, then the value of 'a' is

(A) 1   (B) -1

(C) 2   (D) -2

25. If in triangle ABC, $A \equiv (1, 10)$, circumcentre $\equiv \left(-\dfrac{1}{3}, \dfrac{2}{3}\right)$ and orthocentre $\equiv \left(\dfrac{11}{3}, \dfrac{4}{3}\right)$, then the co-ordinates of mid-point of side opposite to A is

(A) $\left(1, -\dfrac{11}{3}\right)$ (B) $(1, 5)$

(C) $(1, -3)$ (D) $(1, 6)$

PHYSICS – (PART – C)

This part contains **3 Multiple Choice Multi Correct Type Questions** number **26 to 28**. Each question has 4 choices (A), (B), (C) and (D), out of which **MORE THAN ONE** are correct.

26. At time t = 0, car moving along a straight line has a velocity of 16 m/s. It slows down with an acceleration of $-0.5t \ m/s^2$, where t is in second. Mark the correct statement(s):
    (A) The direction of velocity changes at t = 8 sec
    (B) The distance travelled in 4 sec is 58.67 m
    (C) The distance travelled by the particle in 10 sec is 94 m
    (D) The velocity at t_4 = 10 sec is - 9 m/s

27. The figure shows a pulley mass system (assume mass of pulley and string is negligible) which is kept in an elevator that is moving upward with an acceleration a = g. Then
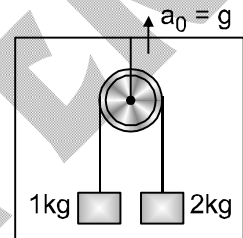
    (A) tension in string is $\dfrac{8}{3}g$

    (B) tension in string is $\dfrac{7}{3}g$

    (C) acceleration of 1 kg mass with respect to ground is $\dfrac{4}{3}g$

    (D) acceleration of 1 kg mass with respect to ground is $\dfrac{5}{3}g$

28. Two blocks of masses 10 kg and 20 kg are connected by a light spring as shown. A force of 200 N acts on the 20 kg mass as shown. At a certain instant the acceleration of 10 kg mass is $12 \ ms^{-2}$.
    (A) At that instant the 20 kg mass has an acceleration of $12 \ ms^{-2}$.
    (B) At that instant the 20 kg mass has an acceleration of $4 \ ms^{-2}$.
    (C) The stretching force in the spring is 120 N.
    (D) The collective system moves with a common acceleration of $30 \ ms^{-2}$ when the extension in the connecting spring is the maximum.

MATHEMATICS – (PART – D)

This part contains **2 Multiple Choice Multi Correct Type Questions** number **29 to 30**. Each question has 4 choices (A), (B), (C) and (D), out of which **MORE THAN ONE** are correct.

29. If $\cos(x-y)$, $\cos x$ and $\cos(x+y)$ are in H.P., then $\cos x \sec\left(\dfrac{y}{2}\right) =$
    (A) $-\sqrt{3}$ (B) $-\sqrt{2}$
    (C) $\sqrt{2}$ (D) $\sqrt{3}$

30. Difference between maximum and minimum values of $(60 \sin\alpha + p\cos\alpha)$ is 122 then p can be
    (A) 61   (B) 11
    (C) – 61   (D) – 11

Section – III

Time: 30 Minutes

CHEMISTRY – (PART – A)

*This part contains **8 Multiple Choice Questions** number **31 to 38**. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.*

31.   A 0.5 g sample of dichromate ore requires 20 ml of 0.22 M ferrous ammonium sulphate for complete reduction. The percentage of chromium in the sample is
(A) 15.25% (B) 20.5%
(C) 30.5% (D) 61%

32.   Ammonia gas in equilibrium with 1 : 3 molar mixture of N_2 and H_2 gases at 50 atm and 400ºC is 20% by weight. The value of equilibrium constant (Kp) for the formation of ammonia will be
(A) 75×10^{-6} (B) 80×10^{-6}
(C) 92×10^{-6} (D) 10×10^{-6}

33.   Out of CO_2, SiO_2, GeO_2, SnO_2 and PbO_2
(A) CO_2 and SiO_2 are acidic, SnO_2 is amphoteric and PbO_2 is an oxidizing agent
(B) PbO_2 is converted to $Pb(NO_3)_2$, on reaction with HNO_3
(C) both (A) and (B) are correct
(D) none is correct

34.   Two moles of an equimolar mixture of two alcohols, $R_1 – OH$ and $R_2 – OH$ are esterified with one mole of acetic acid. If 80% of the acid is consumed and the quantities of ester formed under equilibrium are in the ratio of 3: 2, the value of the equilibrium constant for the esterification of $R_1 –OH$ with acetic acid is
(A) ~ 3.3 (B) ~ 3.7
(C) ~ 3.5 (D) ~ 3.9

35.   A photon of wavelength 300 nm is absorbed by a gas and then remitted as two photons. One photon is red with wavelength of 760 nm. The wave number of the second photon will be
(A) 2.02×10^6 m^{-1} (B) 3.02×10^6 m^{-1}
(C) 1.02×10^6 m^{-1} (D) 2.2×10^6 m^{-1}

36. $CaCO_3$ and $BaCO_3$ have solubility product values 1×10^{-8} and 5×10^{-9} respectively. If water is shaken up with both solids till equilibrium is reached, the concentration of CO_3^{2-} ions is
(A) 1.5×10^{-8} M (B) 1.225×10^{-4}M
(C) 2.25×10^{-9} M (D) none of these

37.   Element having highest ionization potential among the following is?
(A) Al (B) Ga
(C) In (D) Tl

38.   A partially dried clay mineral contains 8% water. The original sample contained 12% water and 45% silica. The percentage of silica in the partially dried sample is nearly
(A) 50% (B) 49%
(C) 51% (D) 47%

CHEMISTRY – (PART – B)

*This part contains **4 Multiple Choice Multi Correct Type Questions** number **39 to 42**. Each question has 4 choices (A), (B), (C) and (D), out of which **MORE THAN ONE** are correct.*

39. The correct statement about the compound(s) (I) and (II) are
    (A) I show geometrical isomerism
    (B) II shows geometrical Isomerism
    (C) I and II are diastereomers
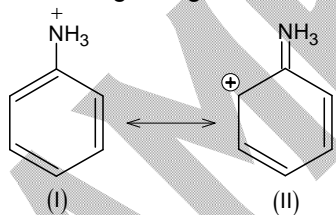   (D) I can show optical isomerism
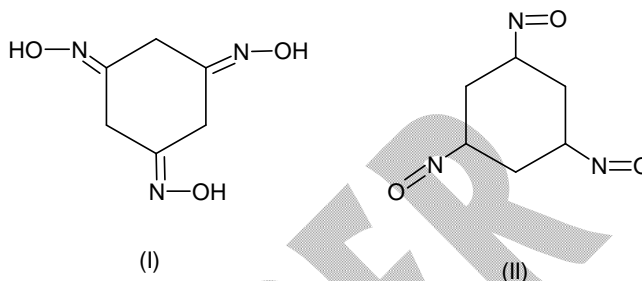
40. Which of the following carbocations is/are likely to show rearrangement?

    (A)

    (B)

    (C)

    (D)
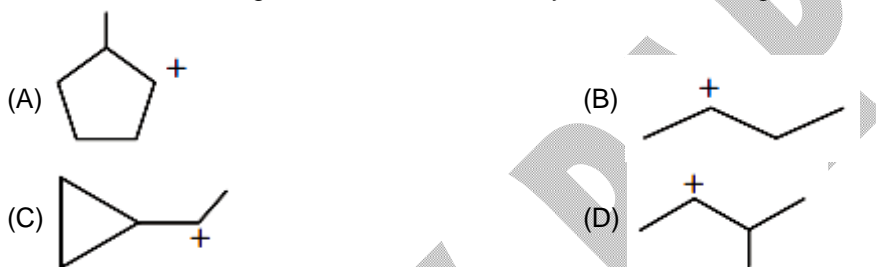
41. Which of the following hydrides are ionic?
    (A) CaH_2
    (B) BaH_2
    (C) SrH_2
    (D) BeH_2

42. Examine the following two structures for the anilinium ion, predict which of the following statement is false regarding the two canonical structures for anilinium ion?

    (I)   (II)

    (A) II is not an acceptable canonical structure because carbocation is less stable than ammonium ions.
    (B) II is not acceptable canonical structure because nitrogen has 10 valence electrons.
    (C) II is not acceptable canonical structure because it is non-aromatic
    (D) II is acceptable structure

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SAMPLE PAPER

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Paper 4 Mathematical Olympiad, Physics & Astronomy Olympiad & Chemistry Olympiad

Paper Code: 1112-4

ANSWER KEY

1.	D	2.	D	3.	D	4.	C
5.	A	6.	A	7.	A	8.	B
9.	A	10.	C	11.	A, C	12.	A, B, C
13.	C, D	14.	A, D	15.	A, B	16.	B
17.	A	18.	A	19.	B	20.	A
21.	A	22.	D	23.	D	24.	D
25.	D	26.	A, B, C, D	27.	A, D	28.	B, C
29.	B, C	30.	B, D	31.	A	32.	A
33.	C	34.	B	35.	A	36.	B
37.	D	38.	D	39.	A, B	40.	A, C, D
41.	A, B, C	42.	A, C, D				